MACQUARIE UNIVERSITY
DIVISION OF ECONOMIC AND FINANCIAL STUDIES
UNIT OUTLINE

ACST356 Mathematical Theory of Risk
FIRST SEMESTER 2007

Unit convenor: Leonie Tickle
Prerequisites: STAT 272 (P)

Students in this unit should read this unit outline carefully at the start of semester. It contains important information about the unit. If anything in it is unclear, please consult the unit convenor.

ABOUT THIS UNIT

This unit examines the use of statistical models in the insurance context. Statistical models of the number of claims and the sizes of the claims are studied. These models are used as a basis for the study of risk theory, ruin theory and the effect of reinsurance. The use of no claim discount systems as a method of experience rating is described. Decision theory and simulation are also studied.

This unit relies heavily on your previous study in STAT 272 and you should ensure that you revise STAT 272 if necessary. In particular, you should be familiar with:

- the theory of statistical distributions, including the meaning of a random variable, discrete and continuous random variables, density functions, cumulative density functions;
- basic results relating to expectation, variance, covariance, and moment and cumulant generating functions;
- joint random variables and marginal density functions;
- the use of Normal Distribution and Chi-Squared distribution tables;
- probability theory, including conditional probability; and
- some mathematical techniques and results including integration by parts and the binomial, logarithmic, exponential, and Taylor series approximations.

TEACHING STAFF

Leonie Tickle is the unit convenor and will be taking all of the lectures and tutorials.

Grace Zhao is the teaching administrator for this unit. Administrative questions that are not covered in this unit outline should be directed to the Administration Enquiries account via the Private Mail facility of the website. If the questions are of interest to everyone in the unit, the question and the reply will be posted to the Discussion Board, so you should specifically request if you want your message to remain private.
Questions about unit content should be sent to the Discussion Board of the website or raised during tutorials or lecture breaks.

**CLASSES**

Classes (all of which start in week one) are held:

- **Tuesday**  2 pm – 4 pm  Lecture  W5A T2
- **Wednesday**  11 am – 12 noon  Lecture  E7B T5
- **Wednesday**  12 noon – 1 pm  Tutorial  E7B T5

**REQUIRED AND RECOMMENDED TEXTS AND/OR MATERIALS**

**Required texts**

A set of lecture notes for the first seven weeks of lectures are available for purchase from the Co-op bookshop. Arrangements for other weeks will be advised in classes.

**Optional recommended text**


This book is available from the Macquarie University Co-op Bookshop. Copies are also available in the Reserve section of the library.

**Other useful references**


These texts are available in the library, with a single copy of each also available in the Reserve section of the library.

**UNIT WEB PAGE**

To access the website, go to [http://online.mq.edu.au](http://online.mq.edu.au) and login using your usual login and password. You will then have access to the websites for all the units in which you are enrolled. If you have any trouble logging in (e.g. you have forgotten your password), please contact the Library Information Customer Service Desk.

Before logging in, you should follow the link labelled “Technical Information” and read all the information there, including the Information Technology Security Policy and Rules and the Information Technology Usage Rules. This technical information also mentions a number of “plugins” that may be required. Of those listed, in this unit you will only need Acrobat Reader.
The website for this unit contains:

- **Unit announcements.** Lecture and other announcements will be posted here.
- **Unit outline.** A copy of this unit outline.
- **Discussion board.** To discuss problems with your fellow students.
- **Private mail.** To contact the unit administrator and for the unit administrator to contact you.
- **Unit notes.** Complete lecture notes for downloading each week.
- **Quizes.** A copy of the lecture quiz for each week of work, with solutions.
- **Assignments.** Assignments 1 and 2 (to be completed online).
- **Tests and exams.** Past class tests and exams with solutions.
- **Revision exercises.** Additional revision questions with solutions.

It is your responsibility to check the website regularly to make sure that you are up-to-date with announcements and with messages sent to your Private Mail address.

Remember to close your browser when you have finished using the site. If you don't, another person can use the still running browser to access the website with your account.

**LEARNING OUTCOMES**

The learning outcomes of this unit are summarised at the start of each section of work. You should revise these after each week to ensure your understanding of the learning objectives.

In addition to the discipline-based learning objectives, all academic programs at Macquarie seek to develop students’ generic skills in a range of areas. One of the aims of this unit is that students develop their skills in the following: *Critical analysis skills; Problem-solving skills; Creative thinking skills.*

**TEACHING AND LEARNING STRATEGY**

The unit material is covered in the three hours of lectures each week. The tutorial is an opportunity for you to attempt questions for each section of work, or to ask the tutor questions. A mock test will be run in the tutorial prior to each of the class tests. In addition to the tutorial, you should use the Discussion Board to ask questions or discuss concepts covered in the unit.

<table>
<thead>
<tr>
<th>Week Number</th>
<th>Week Beginning</th>
<th>Topic Covered</th>
<th>Test / Assign</th>
<th>Tutorial</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>26 February</td>
<td>1. Loss models</td>
<td></td>
<td>Tutorial</td>
</tr>
<tr>
<td>2</td>
<td>5 March</td>
<td>2. Loss models (cont)</td>
<td>Tutorial</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>12 March</td>
<td>2. Estimation and testing fit</td>
<td>Tutorial</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>19 March</td>
<td>2. Estimation and testing fit (cont)</td>
<td>Tutorial</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>26 March</td>
<td>3. Credibility theory</td>
<td>Test 1</td>
<td>Mock test</td>
</tr>
<tr>
<td>6</td>
<td>2 April</td>
<td>4. Reinsurance and deductibles</td>
<td>Lecture</td>
<td></td>
</tr>
<tr>
<td>STUDY BREAK</td>
<td>9 April</td>
<td></td>
<td>Assign 1</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>23 April</td>
<td>5. Introduction to simulation</td>
<td>Tutorial</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>30 April</td>
<td>6. Individual risk model</td>
<td>Tutorial</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>7 May</td>
<td>7. Collective risk model</td>
<td>Tutorial</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>14 May</td>
<td>8. Ruin theory</td>
<td>Test 2</td>
<td>Mock test</td>
</tr>
<tr>
<td>11</td>
<td>21 May</td>
<td>9. Decision theory</td>
<td>Lecture</td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>28 May</td>
<td>10. Decision theory (cont)</td>
<td>Tutorial</td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>4 June</td>
<td>10. Rating; no claim discount</td>
<td>No class</td>
<td></td>
</tr>
</tbody>
</table>
RELATIONSHIP BETWEEN ASSESSMENT AND LEARNING OUTCOMES

This unit is assessed using two class tests and a final examination. This is suitable given the problem-solving and technical nature of the unit. It is also to encourage you to revise the material regularly, since the unit is challenging and demanding.

Tests

Each test is worth 9% of the final assessment for the unit.

- Test 1 will be held Tuesday 3 April at 2 pm. It will cover Sections 1, 2 and 3.
- Test 2 will be held Tuesday 22 May at 2 pm. It will cover Sections 4, 5, 6, 7 and 8.

A Formulae Sheet will be provided in the class tests. No other reference material is permitted.

You should contact the unit coordinator immediately (ie. in most cases, in advance) if unexpected ill–health or other disruption affects your preparation for or performance in a class test. Applications for special consideration due to documented illness or unavoidable disruption must then be made on the “Advice of Absence or other Circumstances” form, available from [http://www.reg.mq.edu.au/academic-index.htm](http://www.reg.mq.edu.au/academic-index.htm), and submitted to the Student Enquiry Service on Level 1 of the Lincoln Building. In the case of illness, this form must be accompanied by the Professional Authority Form.

Exam

The final examination is worth 75% of the final assessment for the unit.

A Formulae Sheet will be provided in the final exam. No other reference material is permitted. You should familiarise yourself with the information in the Formulae Sheet and its layout prior to the examination (a copy is provided at the start of the first set of lecture notes).

The University Examination period in First Half Year 2007 is from 13 June to 29 June. You are expected to present yourself for examination at the time and place designated in the University Examination Timetable. The timetable will be available in Draft form approximately eight weeks before the commencement of the examinations and in Final form approximately four weeks before the commencement of the examinations from [http://www.timetables.mq.edu.au/exam](http://www.timetables.mq.edu.au/exam).

The only exception to not sitting an examination at the designated time is because of documented illness or unavoidable disruption. In these circumstances you may wish to consider applying for Special Consideration. Information about unavoidable disruption and special consideration is available from the 2007 Handbook, Bachelor Degree Rules 7 and 9. Forms to apply for special consideration are available at [http://www.reg.mq.edu.au/academic-index.htm](http://www.reg.mq.edu.au/academic-index.htm).

If a Supplementary Examination is granted as a result of the Special Consideration process the examination will be scheduled after the end of the official examination period. You are advised that it is Macquarie University policy not to set early examinations for individuals or groups of students. All students are expected to ensure that they are available until the end of the teaching semester, that is, the final day of the official examination period.

Test and Examination Rules

Normal examination rules apply to the conduct of tests and the final examination. These rules are set out under the heading “Conduct of Examinations” in the Student Information – Assessment section of the current Macquarie University Handbook of Undergraduate Studies. Students are responsible for familiarising themselves with these rules prior to the class tests and the final examination.
You should ensure that your handwriting in the class tests and in the final examination is legible. Sections of work that are not legible will not be marked.

Academic Senate has resolved that no mobile phones should be brought into examination rooms. Mobile phones must be switched off and sealed in closed bags during class tests.

Calculators will be allowed in the class tests and the final examination but a clear indication of the steps involved in every calculation must be shown. Any machines that have a text-retrieval capacity, whether or not they have a full alphabet on the keyboard, are not allowed. Calculators may be checked at the commencement of class tests and final exam, and the make/model may be recorded.

Dictionaries will not be permitted in the class tests or the final examination.

Applications based on medical grounds (whether for the class tests or final examination) **must** be accompanied by the Professional Authority Form. Applications omitting this form (such as those which only supply a doctor’s certificate) will be ignored.

**Assignments**

There are two assignments in this unit, both to be made available under the Assignments section of the website and to be submitted online.

- Assignment 1 will involve fitting models to data for claim numbers and amounts, based on material covered in sections 1 and 2. It is due 12 noon Wednesday 18 April and is worth 5% of the assessment for the unit.
- Assignment 2 involves simulating a total claims cost using the models developed in Assignment 1, based on the material covered in section 5. It is due 12 noon Wednesday 2 May and is worth 2% of the assessment for this unit.

Although you may discuss general aspects of the assignments with other students, you will be required to certify that the assignments are all your own work, and to provide your detailed working immediately on request if required. Further details of the assignments will be provided in class.

**CLASS ETIQUETTE**

Mobile phones should be switched off during all lectures and tutorials. If there is an important reason for you to keep your phone on you should request to be allowed to do so before the start of the class.

Lectures commence at 5 minutes past the hour and you are expected to be punctual. You are expected to keep talking to a minimum so as not to disrupt your fellow students (and the lecturer!).

**PLAGIARISM**

The University defines plagiarism in its rules: “Plagiarism involves using the work of another person and presenting it as one’s own.” Plagiarism is a serious breach of University rules and carries significant penalties. You must read the University practices and procedures on plagiarism, available in the Handbook or at [http://www.student.mq.edu.au/plagiarism/](http://www.student.mq.edu.au/plagiarism/). Penalties for plagiarism may include a deduction of marks, failure in the unit, and referral to the University Discipline Committee.

**UNIVERSITY POLICY ON GRADING**

Academic Senate has a set of guidelines on the distribution of grades across the range from F to HD. Your final result will include one of these grades plus a standardised numerical grade (SNG).
On occasion your raw mark for a unit (i.e., the total of your marks for each assessment item) may not be the same as the SNG which you receive. Under the Senate guidelines, results may be scaled to ensure that there is a degree of comparability across the university, so that units with the same past performances of their students should achieve similar results.

It is important that you realise that the policy does not require that a minimum number of students are to be failed in any unit. In fact it does something like the opposite, in requiring examiners to explain their actions if more than 20% of students fail in a unit. For an explanation of the policy see http://www.mq.edu.au/senate/MQUonly/Issues/Guidelines2003.doc or http://www.mq.edu.au/senate/MQUonly/Issues/detailedguidelines.doc.

**Electronic Communication and Your Student File**

Every business keeps a record of its correspondence with its customers. The University is no exception and it maintains a file for every student. Staff are required to ensure that copies of all correspondence with you are added to your file. Historically, “correspondence” meant letters, but nowadays it also includes electronic communication such as email. Staff have some discretion here and might not file copies of trivial emails, but it is difficult to define precise boundaries here, so it is safer to assume that any email you send to a staff member will be added to your file.

Some people regard email as more ephemeral than a letter and thus tend to take less care with issues such as clarity of expression, grammar and spelling. Before sending an email to a staff member, a good question to ask yourself is: “If a member of staff is reviewing my student file prior to writing a reference for me, and they see a copy of this email, would that staff member gain a favourable impression of my level of communication skills?”

In this context, email includes communications you send to staff with the mail tool in the unit's web site. It does not normally include postings you make to the discussion area. However, in those very rare cases where a student makes an inappropriate posting to the discussion area, a copy of the posting would be added to that student's file.

**Student Support Services**

Macquarie University provides a range of Academic Student Support Services. Details of these services can accessed at http://www.student.mq.edu.au.

**ERIC.** The EFS Resource and Information Centre (ERIC) is located in room E4B106 and offers photocopying facilities, reading areas and reference material.

**ACSTINFO.** This ACSTINFO site is used to distribute information to all students majoring in actuarial studies. The information supplied may include administrative information and job advertisements. You will retain access to this site during the vacation following the end of this semester. It is to your advantage to ensure you read information on this web site regularly. You should not assume that information posted there will also be repeated in lectures. To access the site, go to: http://online.mq.edu.au/pub/ACSTINFO/ (Note that the address is case-sensitive.) When you login to this site, please read the section labelled “How to use this site.” This contains useful information which will help you determine when there is new information on the site which you should read.

**Institute of Actuaries of Australia**

There are advantages to joining the Institute of Actuaries of Australia as a student. Please refer to http://www.actuaries.asn.au/AboutTheInstitute/Membership for information.